

四阶 Runge-Kutta 求解方程组

例: $dx/dt=x+2y$, $x(0)=6$

$dy/dt=3x+2y$, $y(0)=4$ """

```
import numpy as np
```

```
import math as m
```

```
from sympy import *
```

```
import matplotlib.pyplot as plt
```

```
plt.rcParams['font.sans-serif']=['SimHei'] #显示中文标签
```

```
plt.rcParams['axes.unicode_minus']=False
```

```
xarray=[]
```

```
yarray=[]
```

```
array=[]
```

```
def f(x,y):
```

```
    a=x+2*y
```

```
    return a
```

```
def g(x,y):
```

```
    a=3*x+2*y
```

```
    return a
```

```
def RK4():
```

```
    h=0.02
```

```
    a=0
```

```
    x=6
```

```
    y=4
```

```
    while a<=0.2:
```

```
        array.append(a)
```

```
        xarray.append(x)
```

```
        yarray.append(y)
```

```
        a+=h
```

```
        f1=f(x,y) #第一步
```

```
        m1=x+f1*h/2
```

```
        g1=g(x,y)
```

```
        n1=y+g1*h/2
```

```
        f2=f(m1,n1) #第二步
```

```
        m2=x+f2*h/2
```

```
        g2=g(m1,n1)
```

```
        n2=y+g2*h/2
```

```
        f3=f(m2,n2) #第三步
```

```
m3=x+f3*h
g3=g(m2, n2)
n3=y+g3*h
```

```
f4=f(m3, n3) #第四步
g4=g(m3, n3)
```

```
x=x+(f1+2*f2+2*f3+f4)*h/6
y=y+(g1+2*g2+2*g3+g4)*h/6
```

```
def main():
    RK4()
    for i in xarray:
        print(i)
    print("-----")
    for i in yarray:
        print(i)
    plt.figure(12)
    plt.subplot(212)
    plt.scatter(xarray, yarray, alpha=0.6)
    plt.subplot(221)
    plt.scatter(array, xarray, alpha=0.6)
    plt.subplot(222)
    plt.scatter(array, yarray, alpha=0.6)
    plt.show()

if __name__ == "__main__":
    main()
```